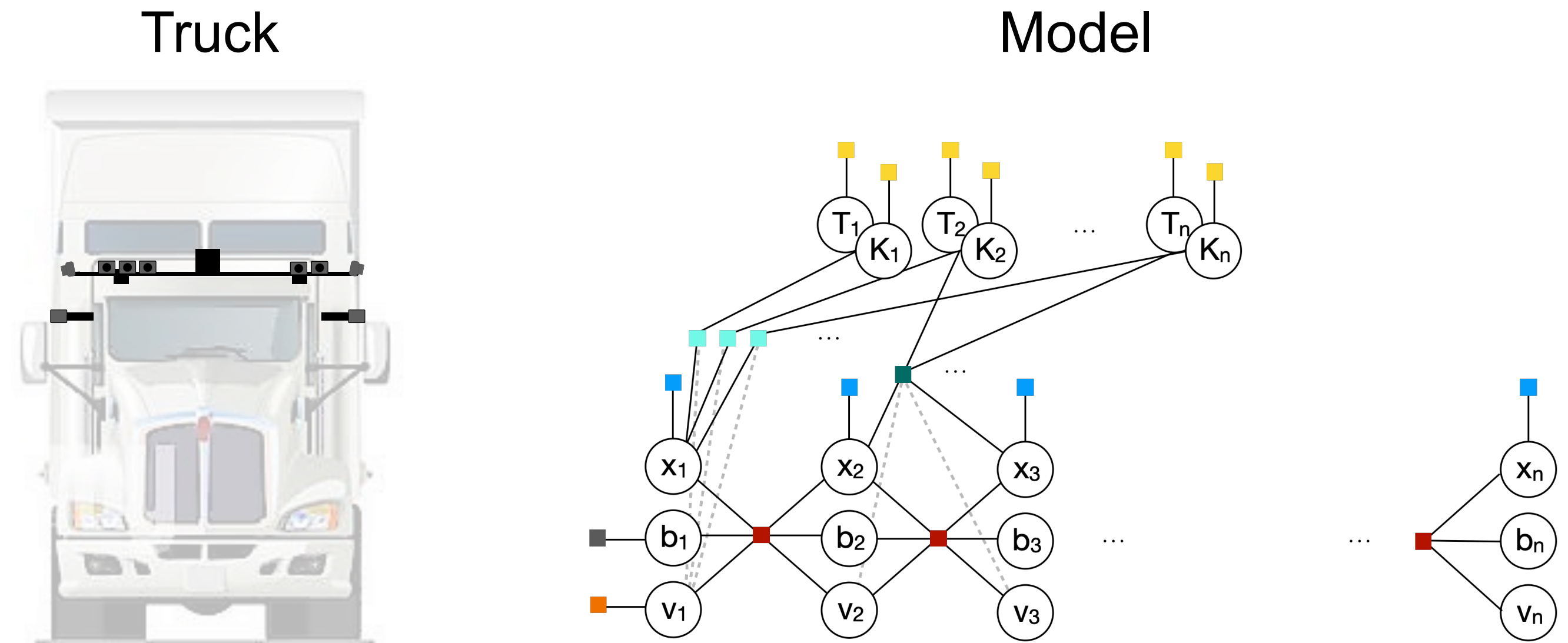


Multi-Sensor Sequential Calibration System at TuSimple

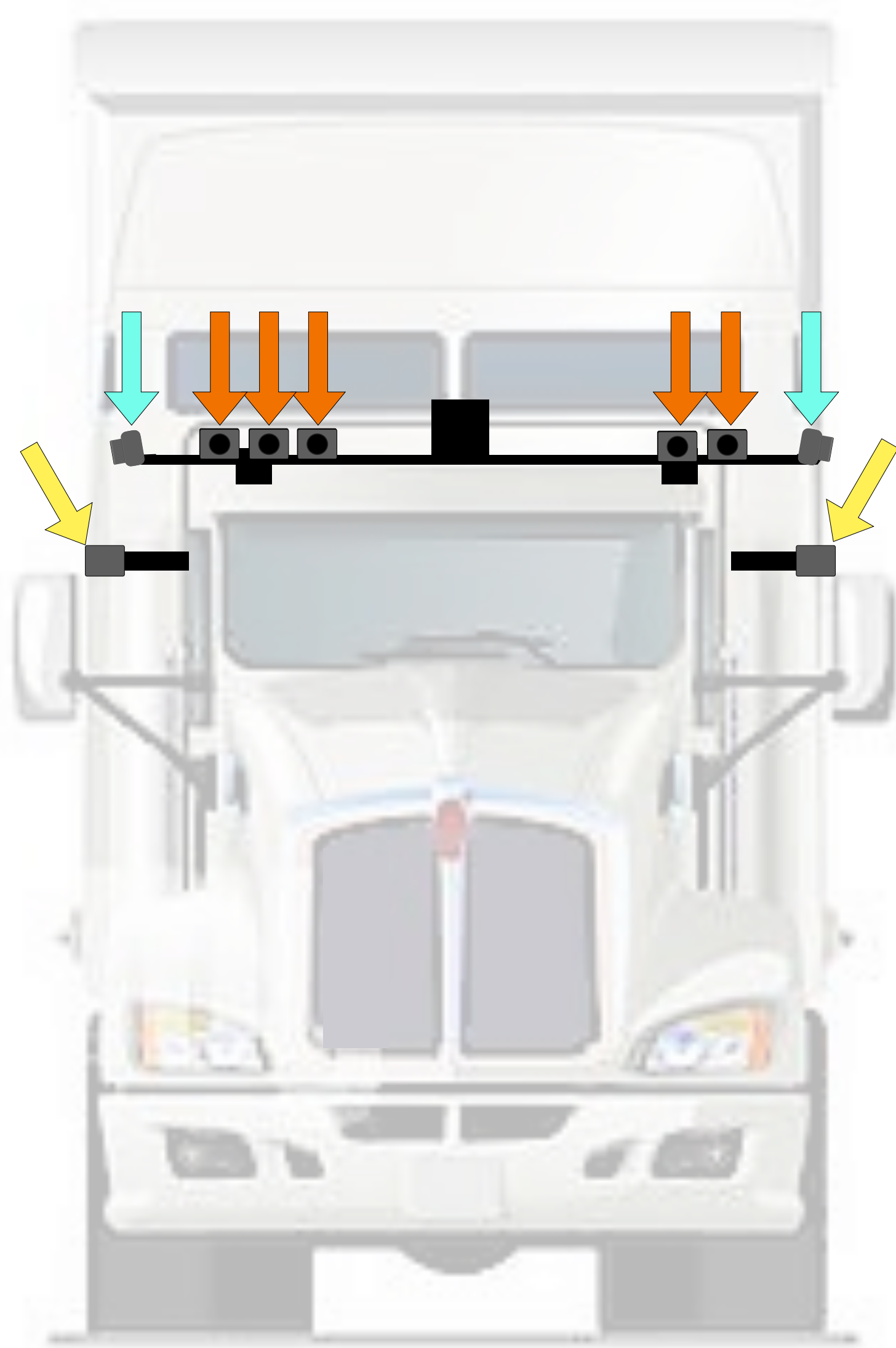
25 min

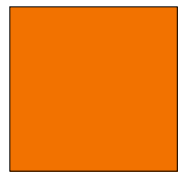
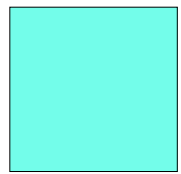
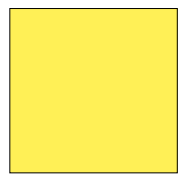
1. Introduction
2. Problem Constraints
3. Basic Model
4. Extensions
5. Evaluation

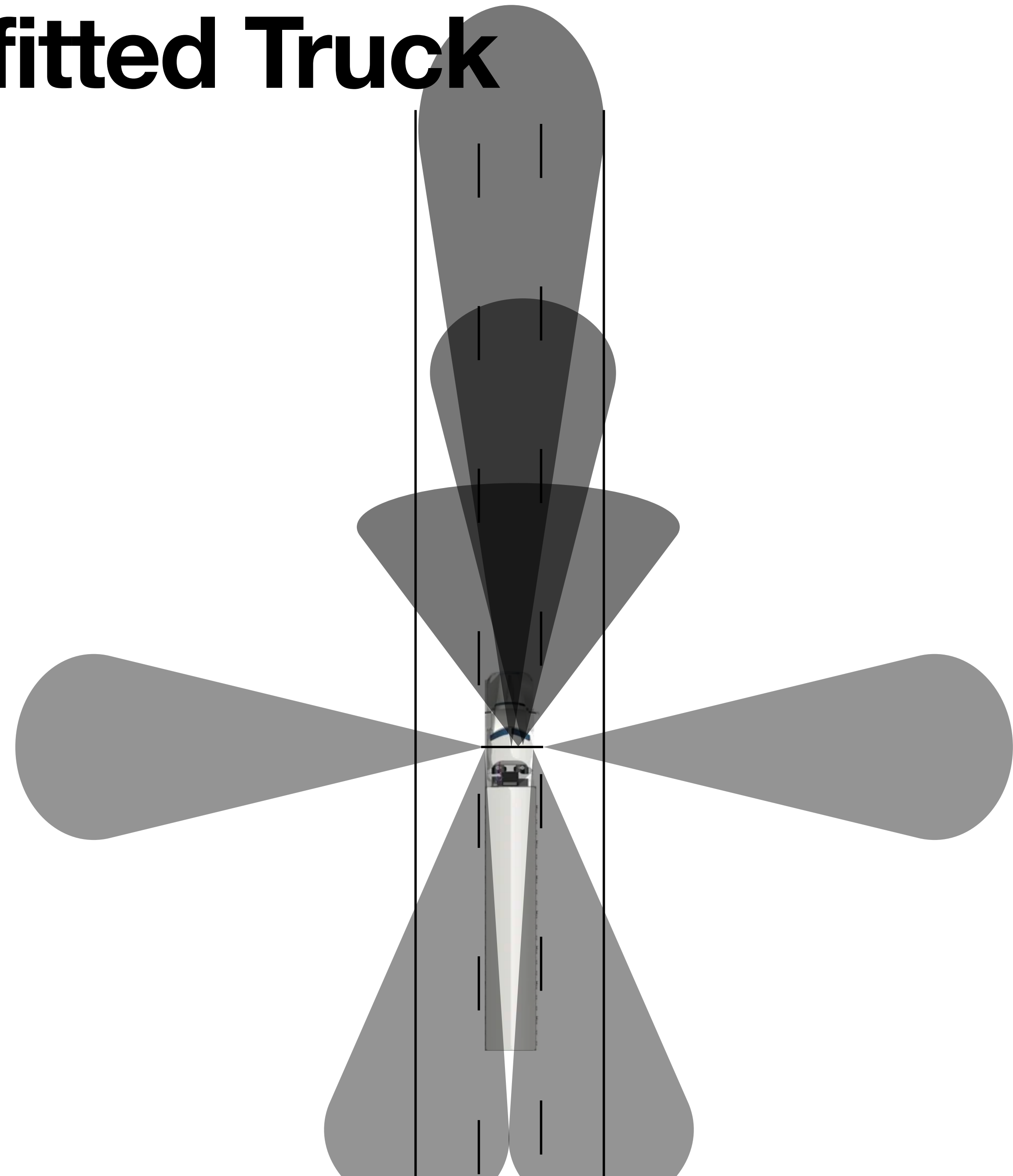


Impact. Delivered in time for a demo of the autonomous driving technology.

1. Introduction: 1. An Outfitted Truck



-  Front-facing
-  Side-facing
-  Rear-facing



1. Introduction: 2. Operational Design Domain

- L4 autonomous truck
- Highway, limited urban driving
- Mapped roads
- Routes are known a priori
- The same routes are repeatedly driven

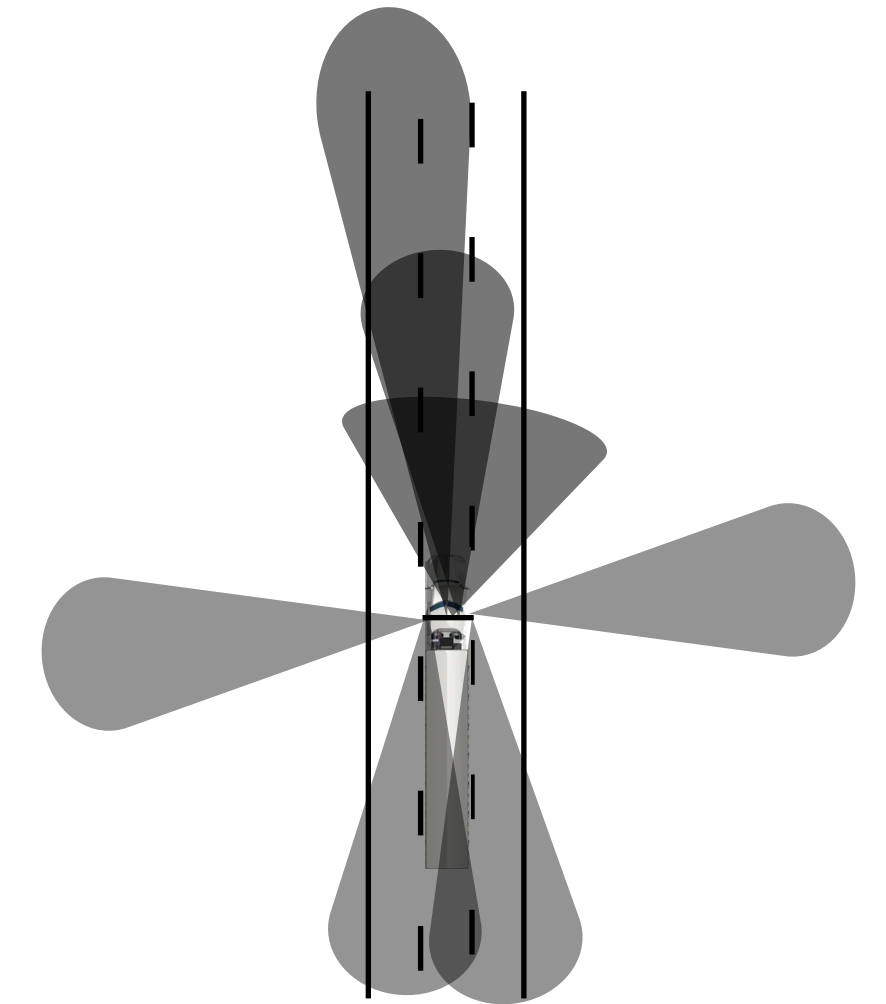
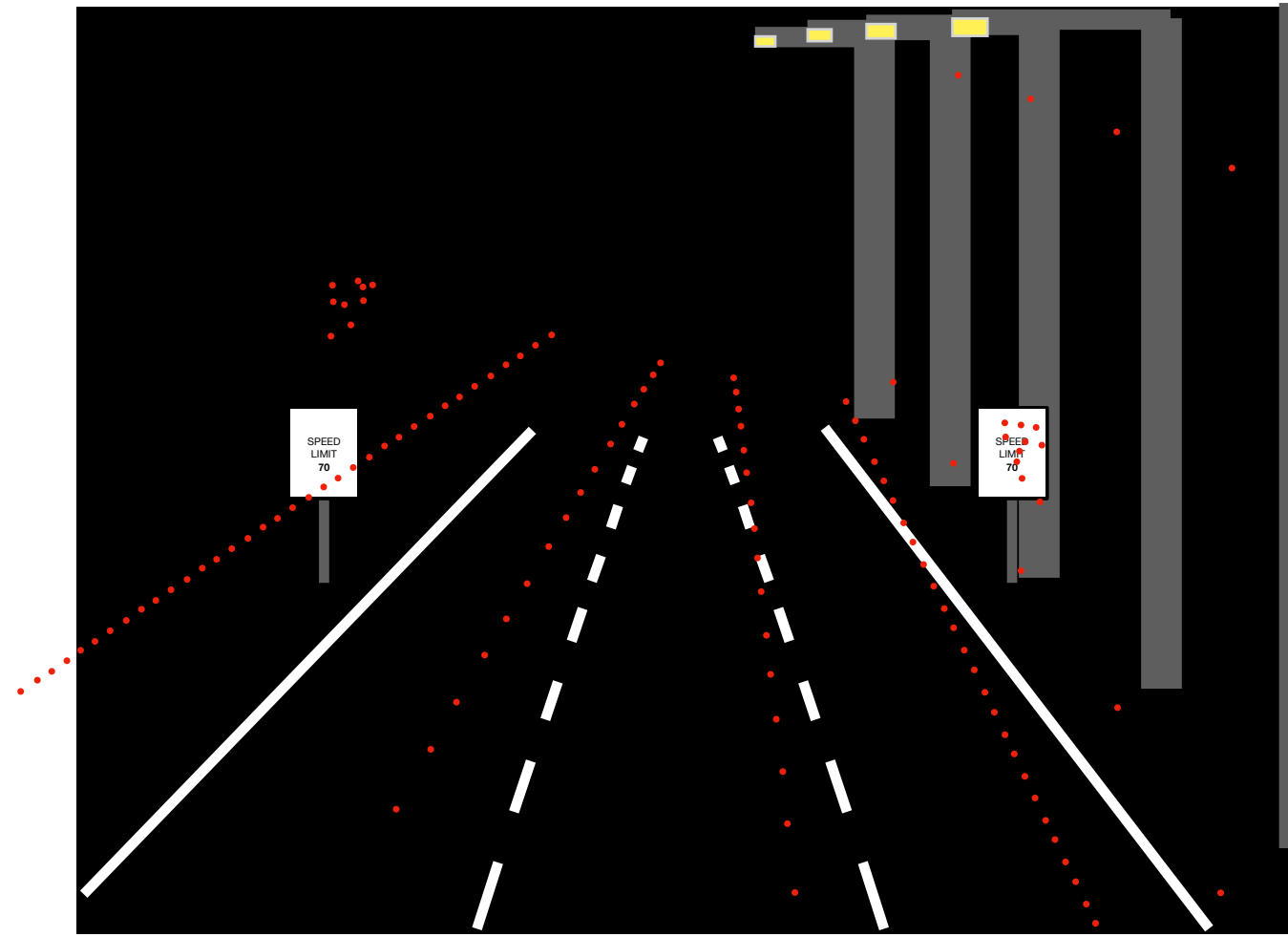


1. Introduction: 3. Extrinsic Camera Calibration

Projection of a prior map onto an image

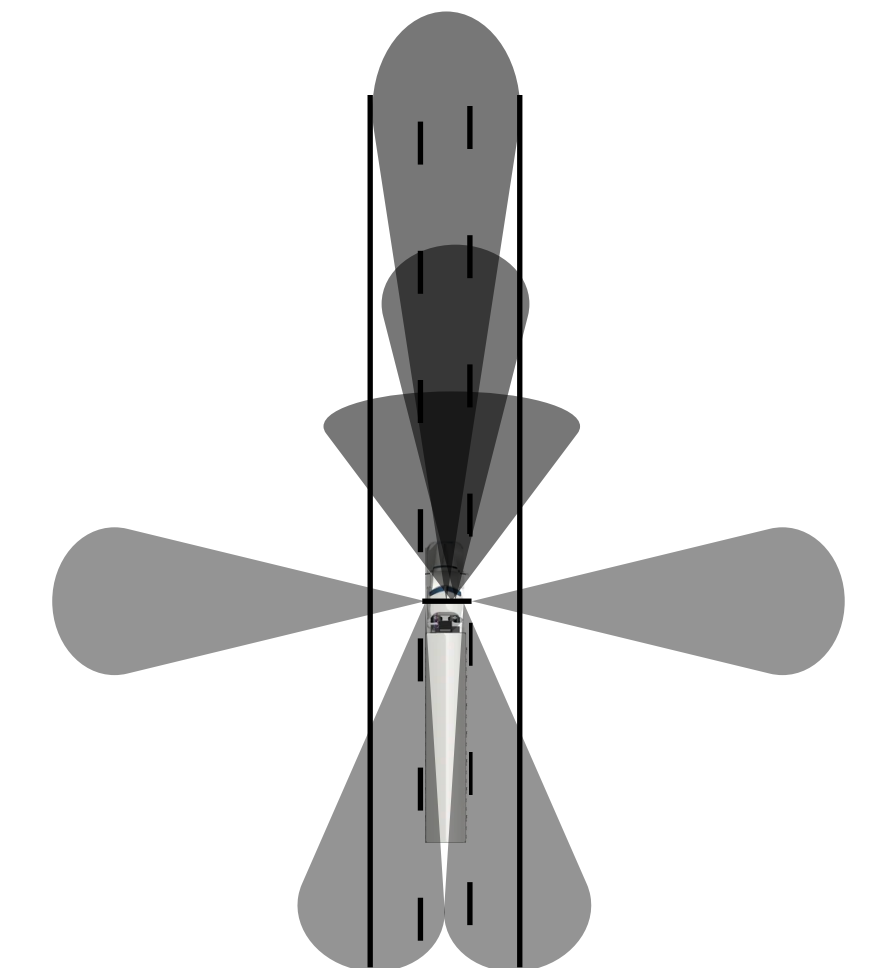
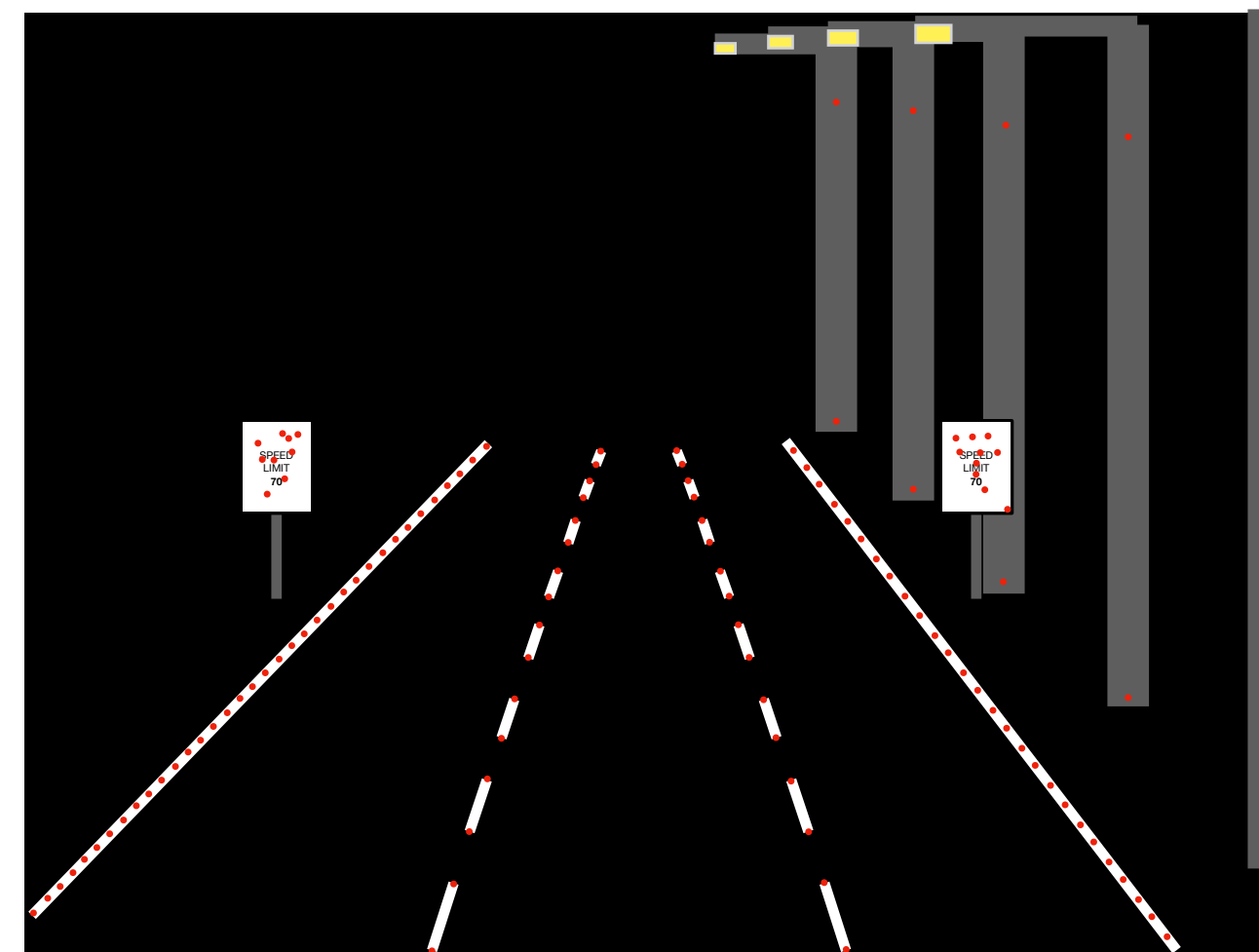
Camera FOVs

Uncalibrated



The goal is accurate SE(3) inter-sensor camera transforms

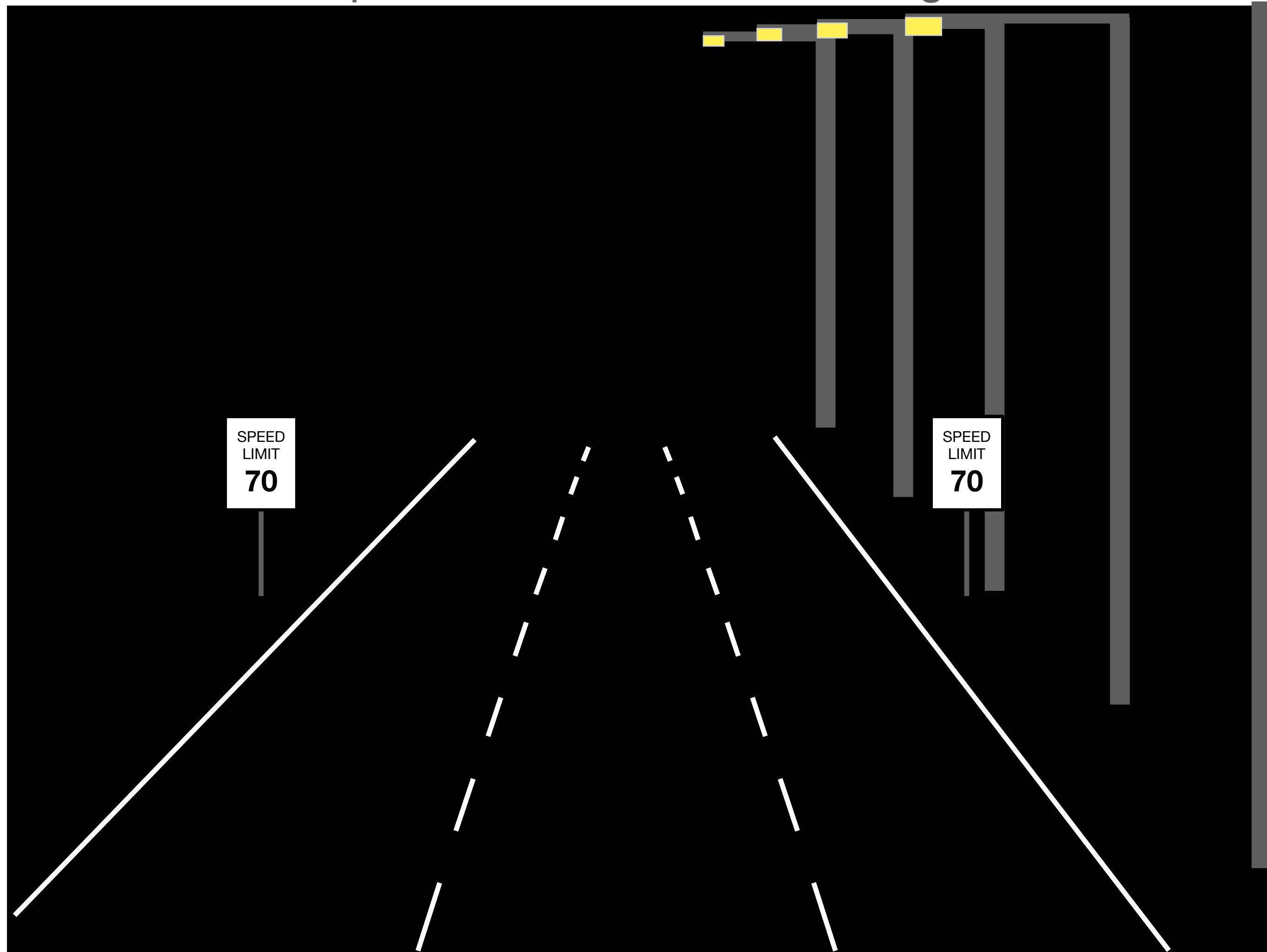
Calibrated



2. Problem Constraints: 1. Calibration Environment

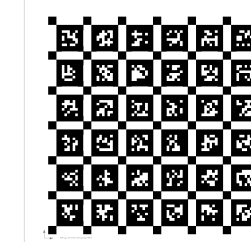
In-Situ Calibration
(this talk)

An example view from one front-facing camera

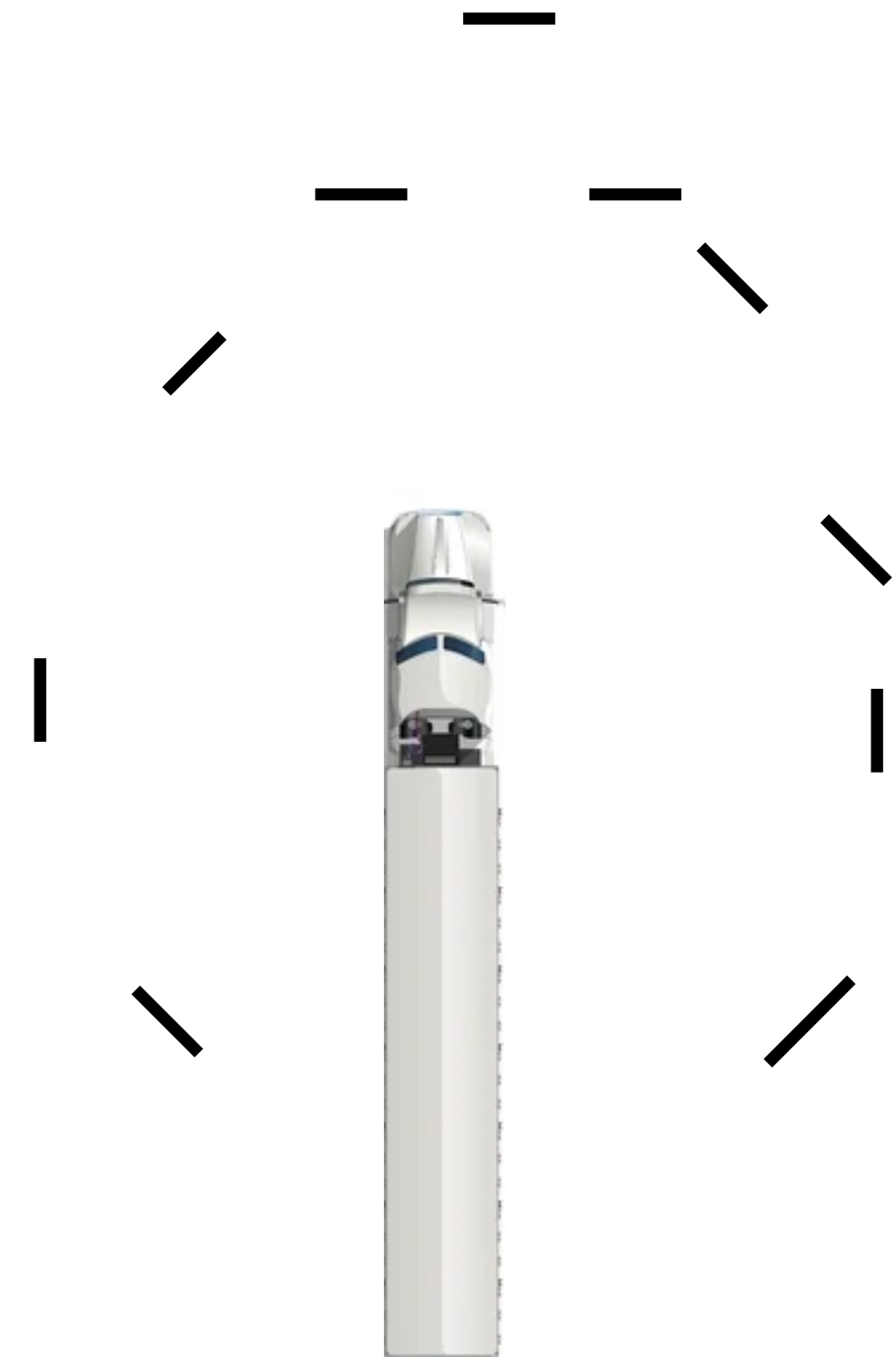


Warehouse calibration

AprilGRID
Calibration Board



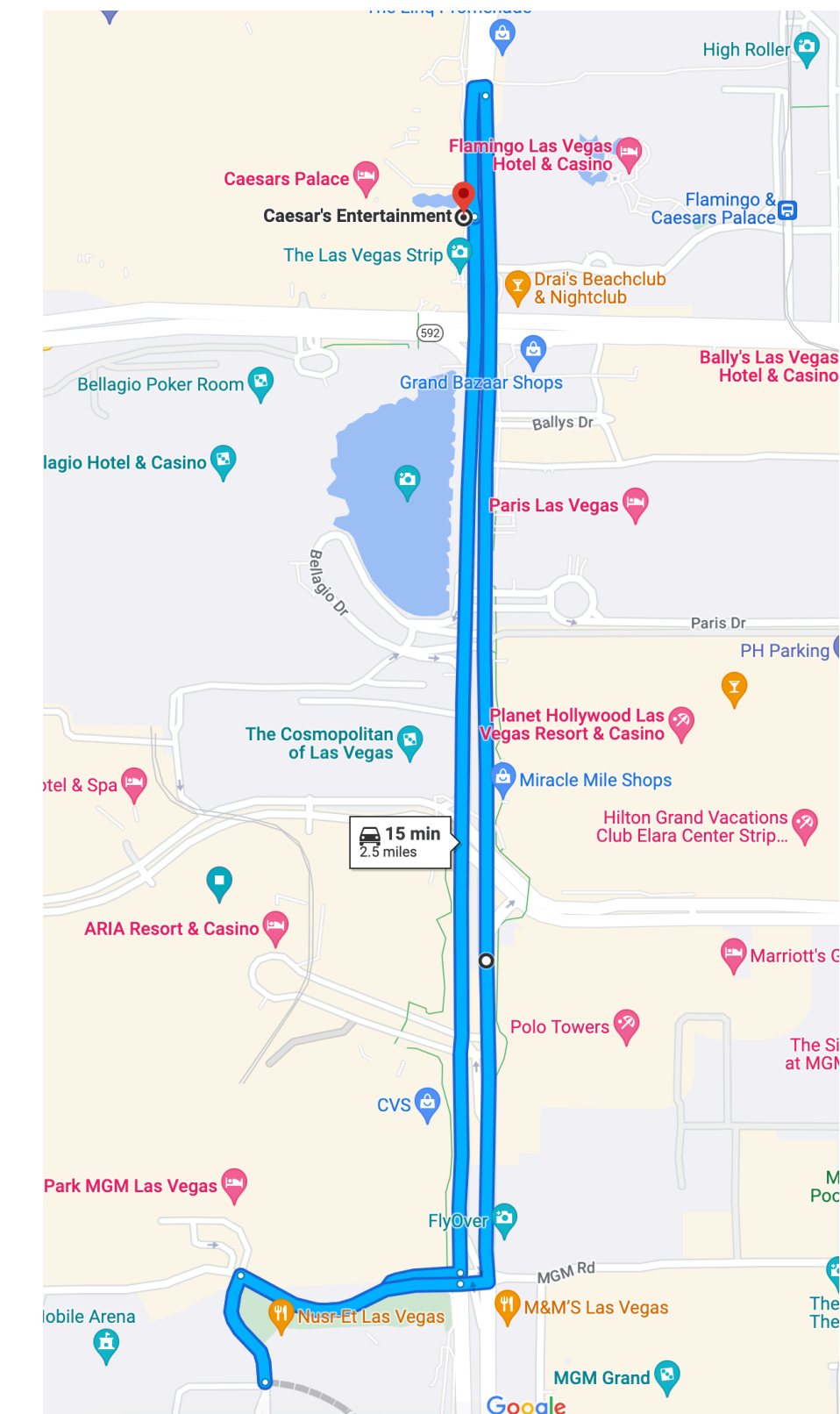
Example layout



2. Problem Constraints: 2. Operations

- A defined, pre-mapped calibration route.
- The vehicle is operated by a licensed driver
- Data collection
- Offline, batch optimization for extrinsic calibration

Example route



2. Problem Constraints: 3. Priors

Camera Extrinsic Priors

$${}^{cam_c}\hat{T}_{imu} \in SE(3)$$

Camera Intrinsics

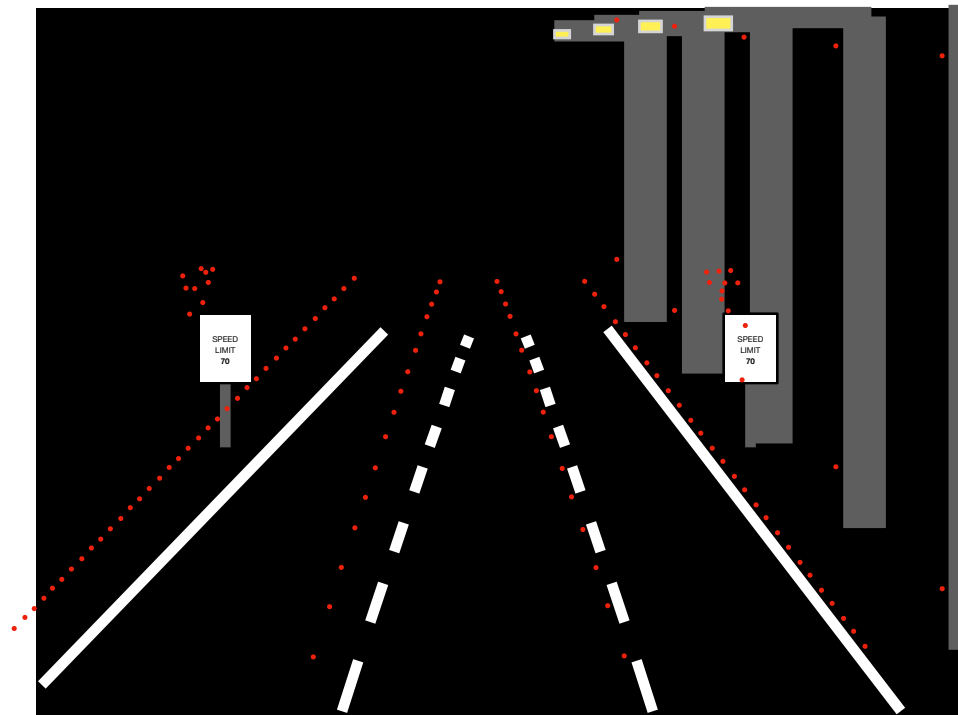
$$K = \begin{pmatrix} f_x & 0 & c_x \\ 0 & f_y & c_y \\ 0 & 0 & 1 \end{pmatrix}$$

$$D = k_1, k_2, k_3, k_4$$

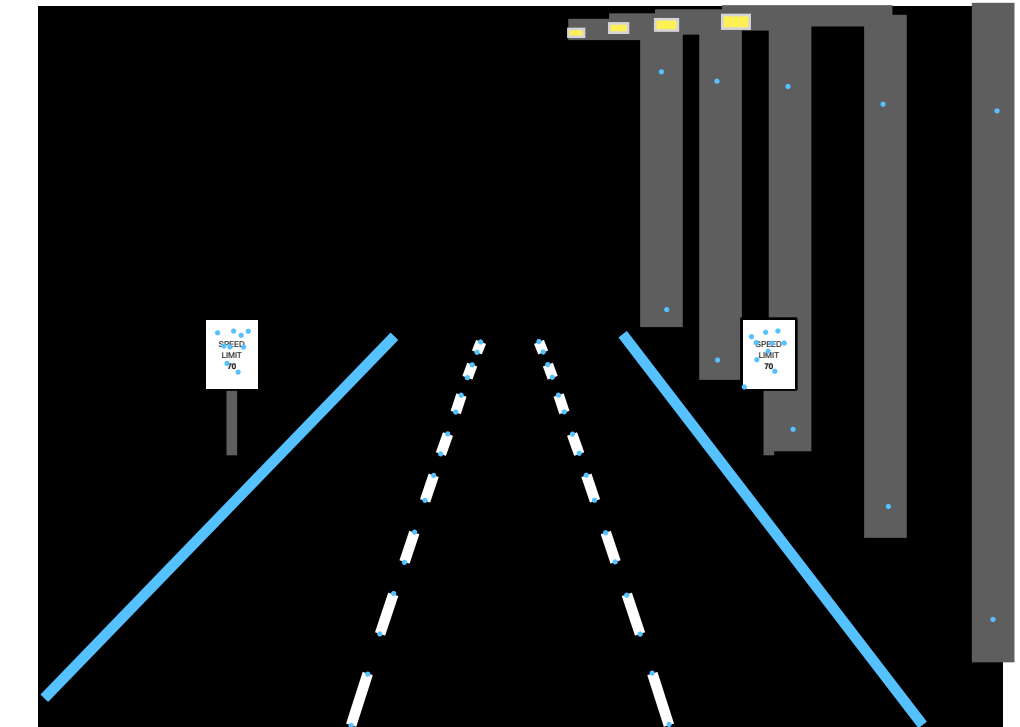
RTK GPS



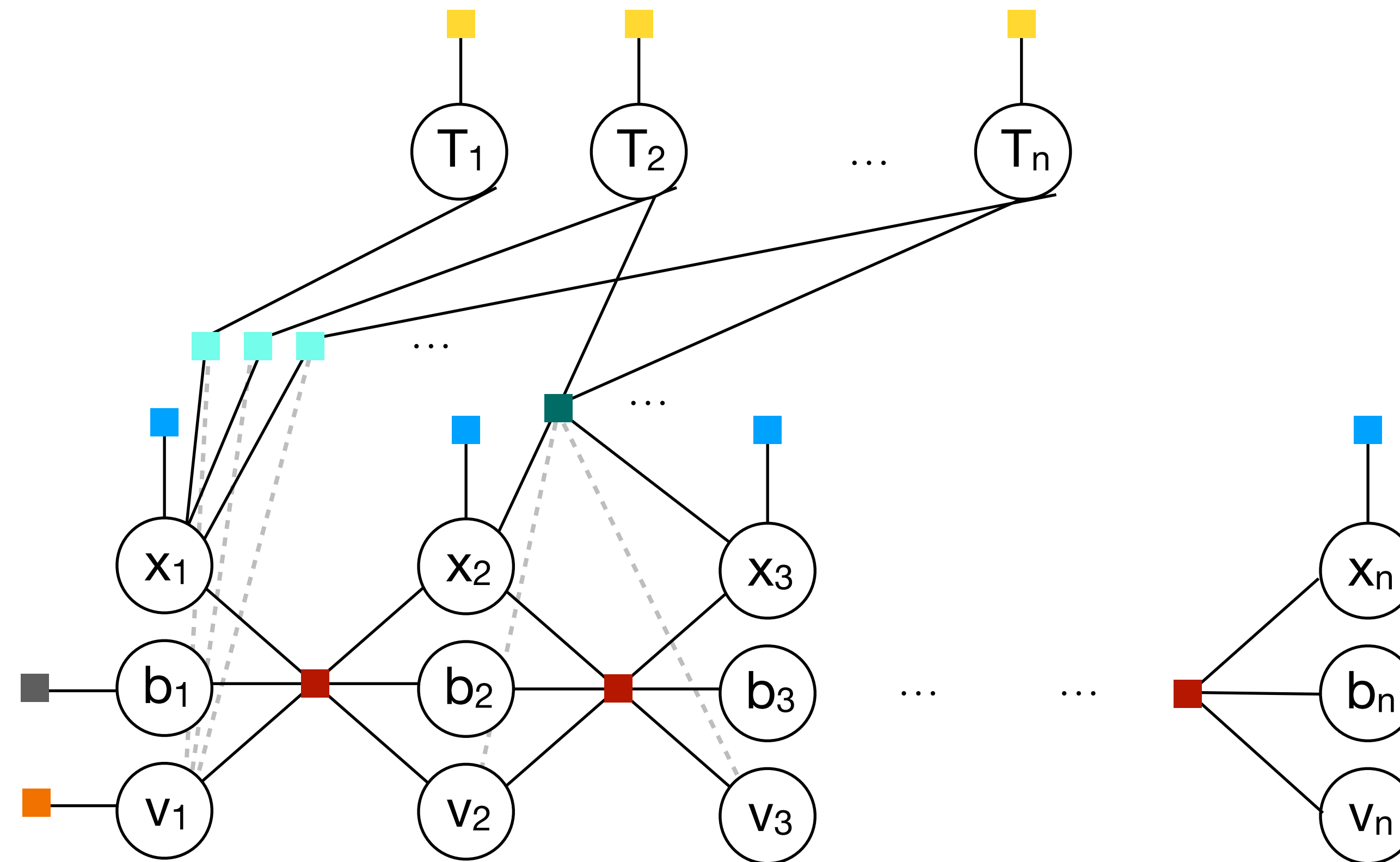
Lane Map



Detections



3. Basic Model: 1. Where we're headed



- | Variables | | Factors | |
|------------------------|------------------|---|-----------------------|
| $T_c \in SE(3)$ | camera extrinsic | ■ Identity prior | ■ IMU preintegration |
| $x_t \in SE(3)$ | vehicle state | ■ GNSS pose prior | ■ 3D-2D projection |
| $b_t \in \mathbb{R}^6$ | IMU bias | ■ velocity prior | ■ 2D-2D epipolar line |
| $v_t \in \mathbb{R}^3$ | velocity | ■ camera extrinsic priors | |
| | | ⋯⋯⋯ used for rolling shutter compensation | |

3. Basic Model: 2. Mathematical Description

Projection Equation

$$p_m^c = K \text{ }^{cam_c}T_{veh} \text{ }^{veh}T_{enu} P_m$$

$$P_m \in \mathbb{R}^3$$

map point

$$\text{}^{veh}T_{enu} \in SE(3)$$

vehicle pose

$$\text{}^{cam_c}T_{veh} \in SE(3)$$

camera extrinsic

$$K \in \mathbb{R}^{3 \times 3}$$

pinhole camera intrinsic

$$p_m^c \in \mathbb{R}^2$$

projected map point

Residual

$$p_d^c - p_m^c$$

$$p_d^c \in \mathbb{R}^2$$

detected 2D point

From e.g., nearest neighbors data association

3. Basic Model: 3. Stationary Formulation

$$\underset{(T_c)_{c \in C}}{\operatorname{argmin}} \sum_{c \in C} \sum_{(d,m)_c} \frac{1}{2} \|p_d^c - h_m(T_c)\|_{\Sigma_m}^2$$

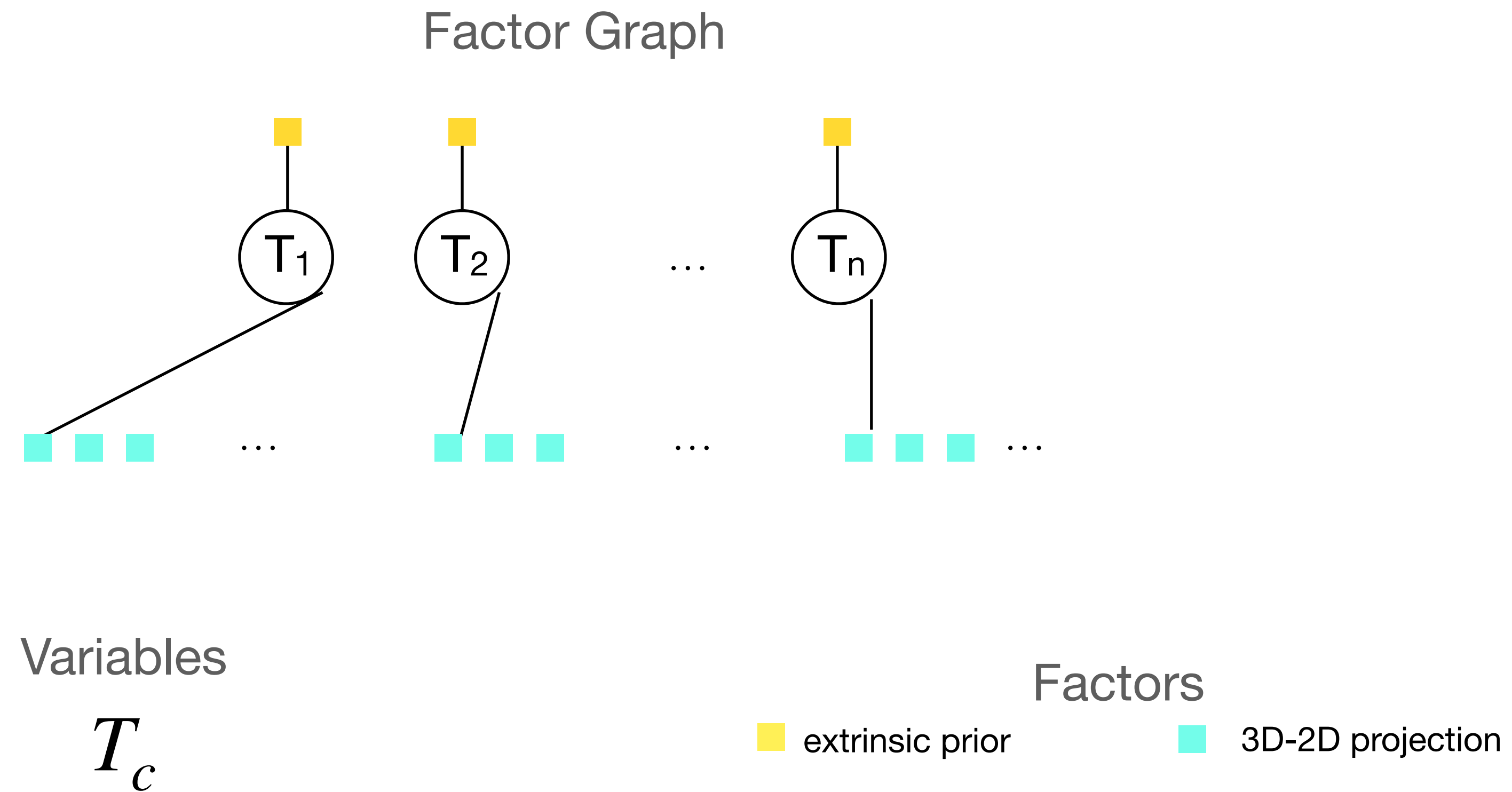
$${}^{cam_c}T_{veh} \longrightarrow T_c$$

shorthand notation

$$\Sigma_m$$

measurement covariance

3. Basic Model: 4. Factor Graph



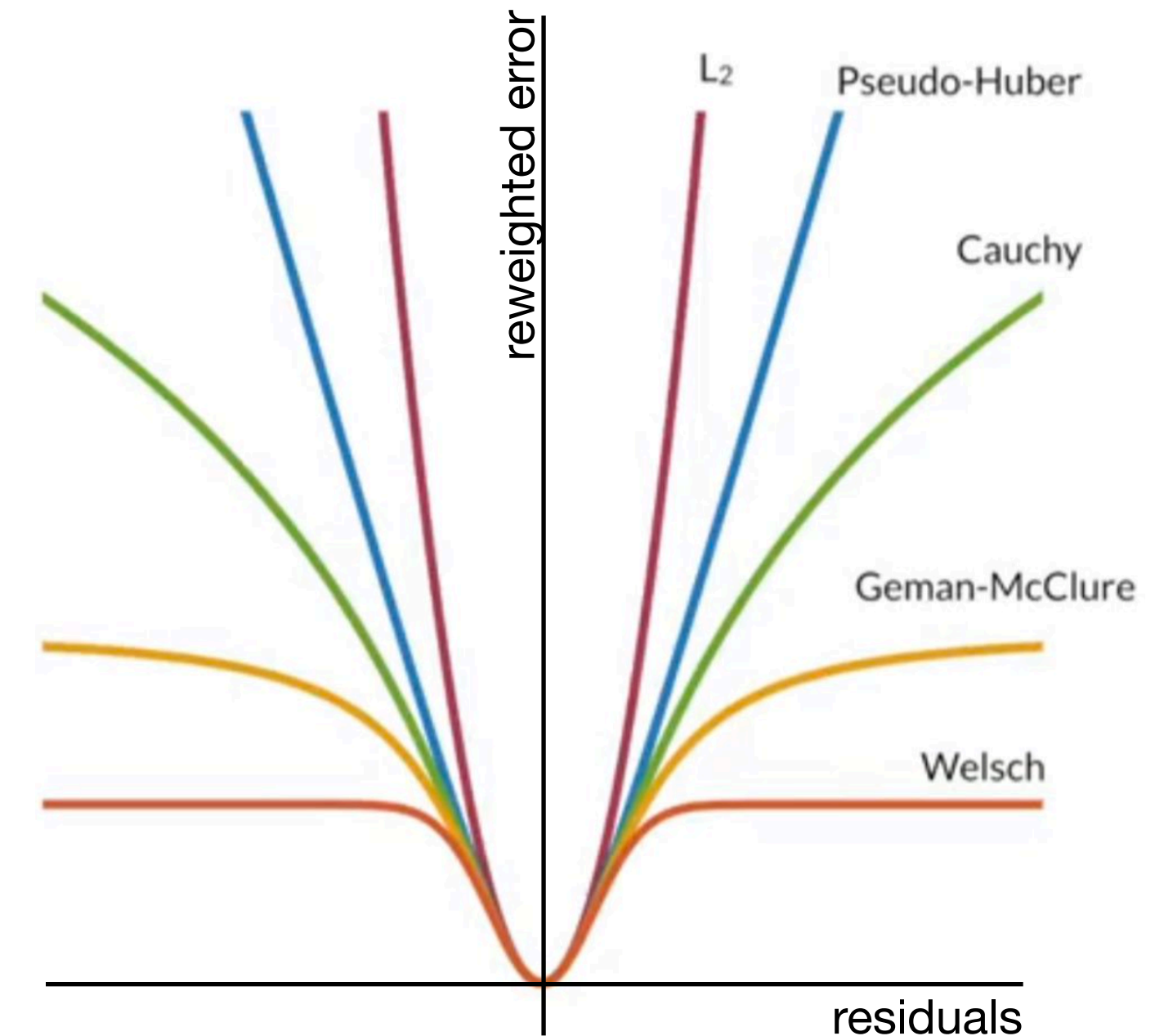
4. Extensions: 1. Robust Noise Model

$$\underset{(T_c)_{c \in C}}{\operatorname{argmin}} \sum_{c \in C} \sum_{(d,m)_c} \tau(|p_d^c - h_m(T_c)|_{\Sigma_m})$$

$\tau()$

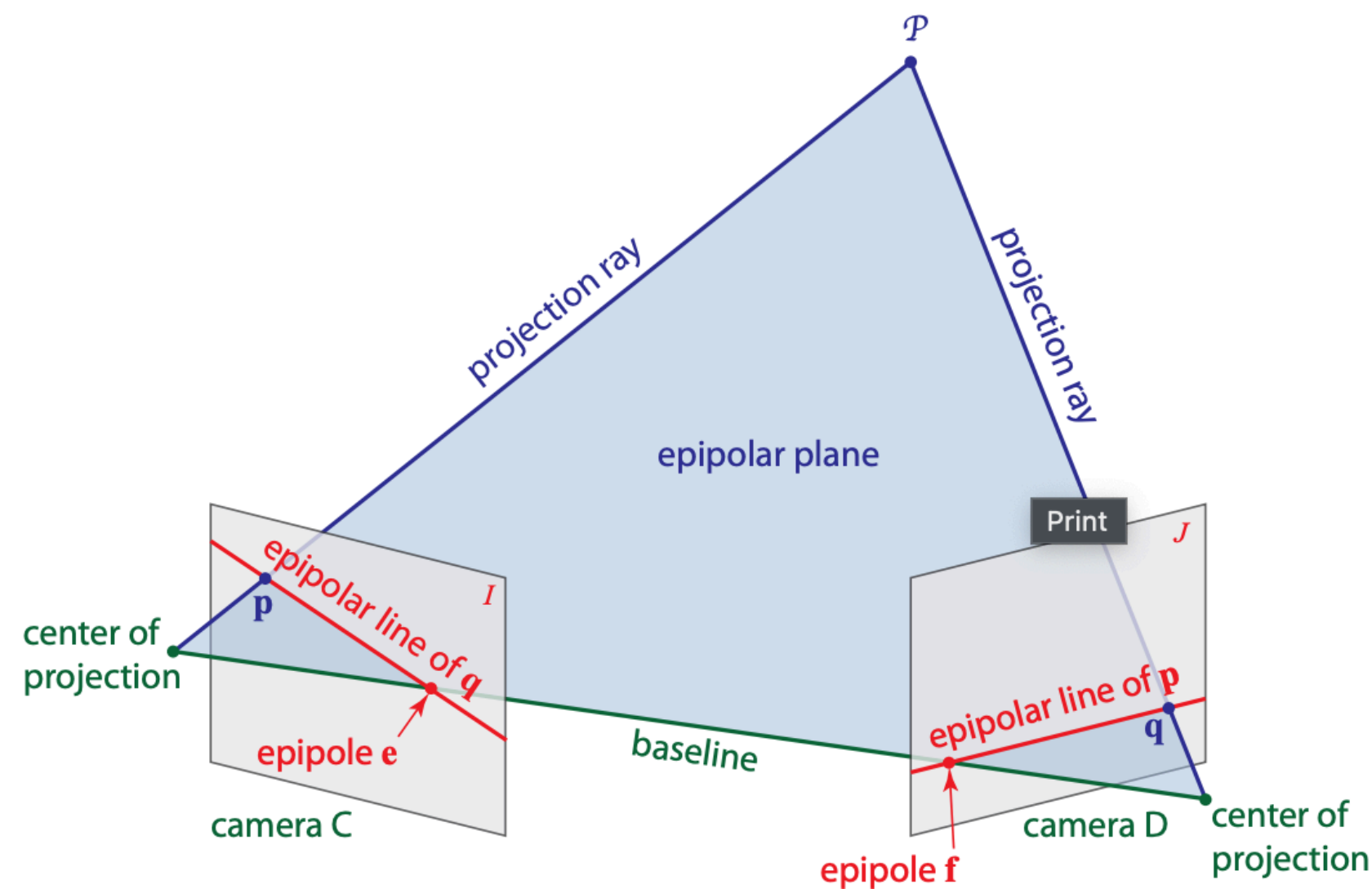
robust loss function

Reweighting functions



4. Extensions: 2. Epipolar Constraint

Geometric Interpretation



Essential Matrix Constraint

$$0 = p_d'^{c1} E p_d'^{c2}$$

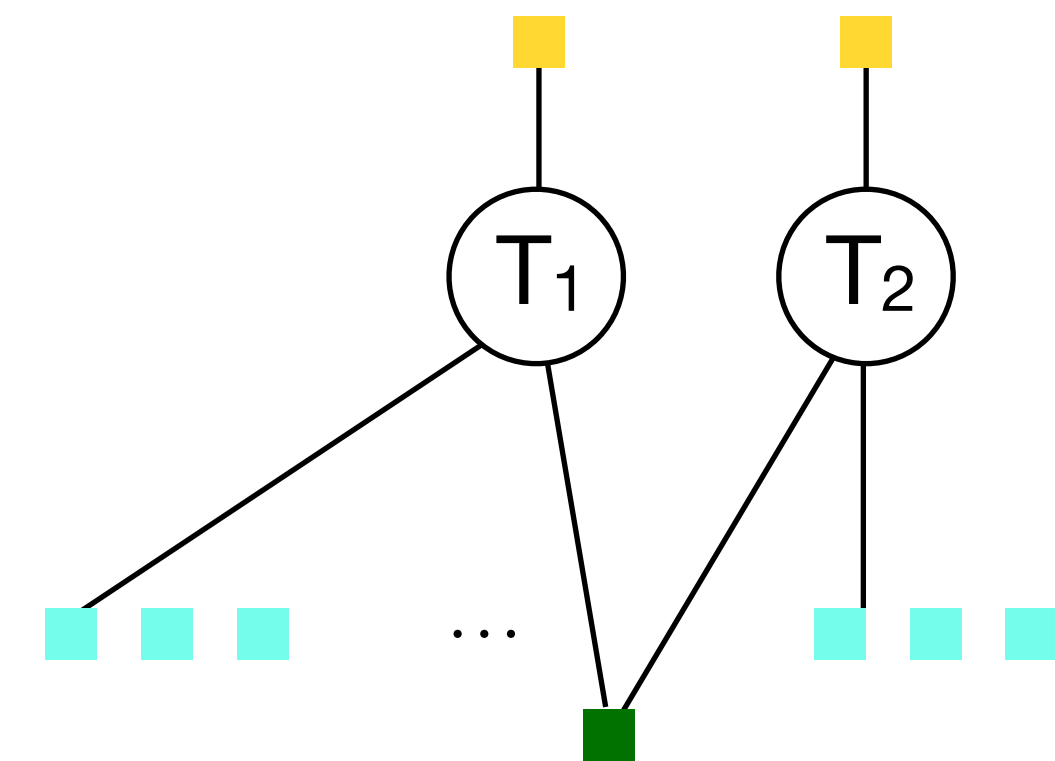
$p_d'^c$ normalized pixel coordinate

$$E = R[t]_x$$

$$t_x = \begin{bmatrix} 0 & -z & y \\ z & 0 & -x \\ -y & x & 0 \end{bmatrix}$$

$${}^{cam_{c1}}T_{cam_{c2}} = \begin{bmatrix} R & t \\ 0 & 1 \end{bmatrix}$$

Factor Graph



Factors

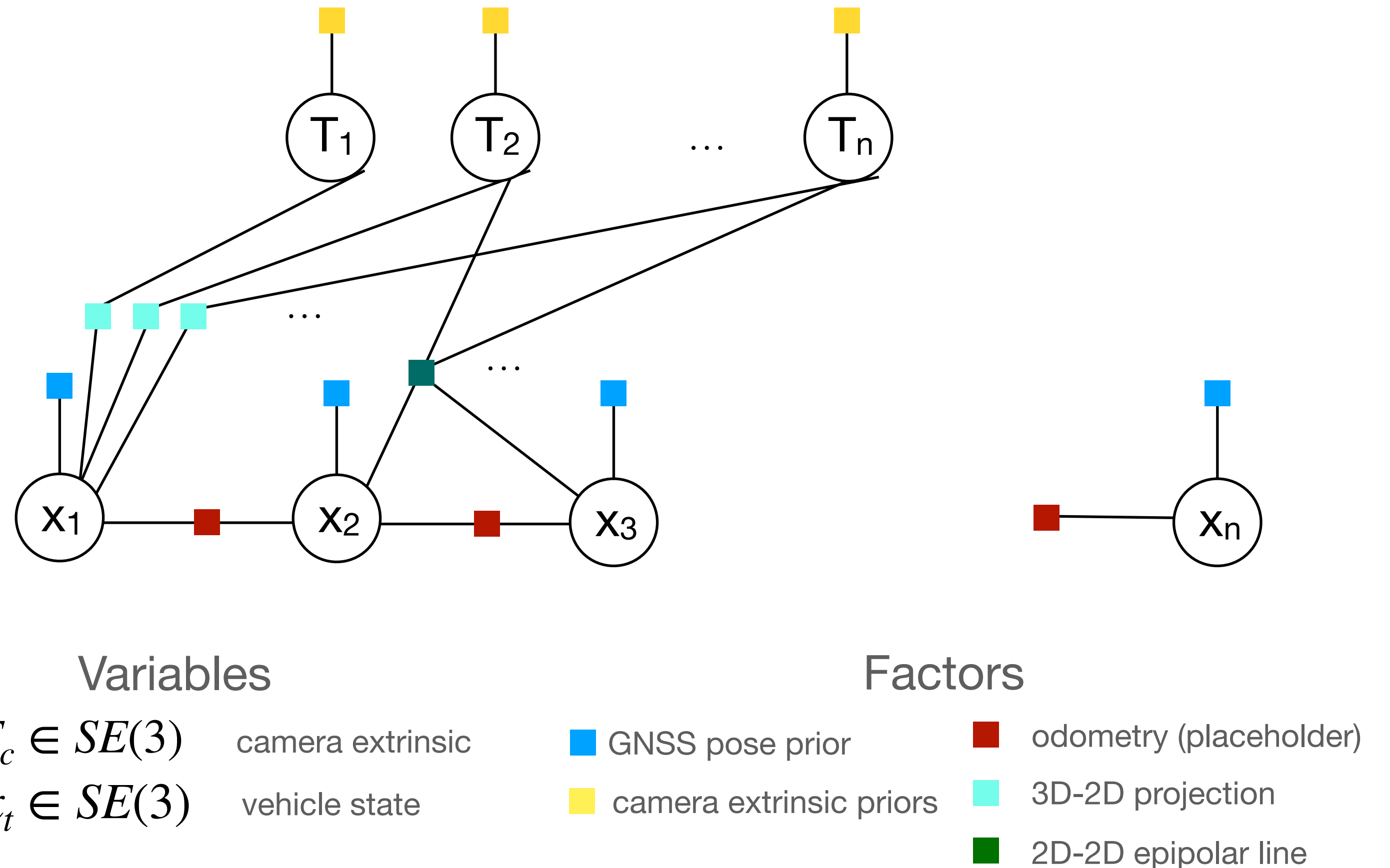
■ extrinsic prior

■ 2D-2D constraint

■ 2D-2D epipolar line

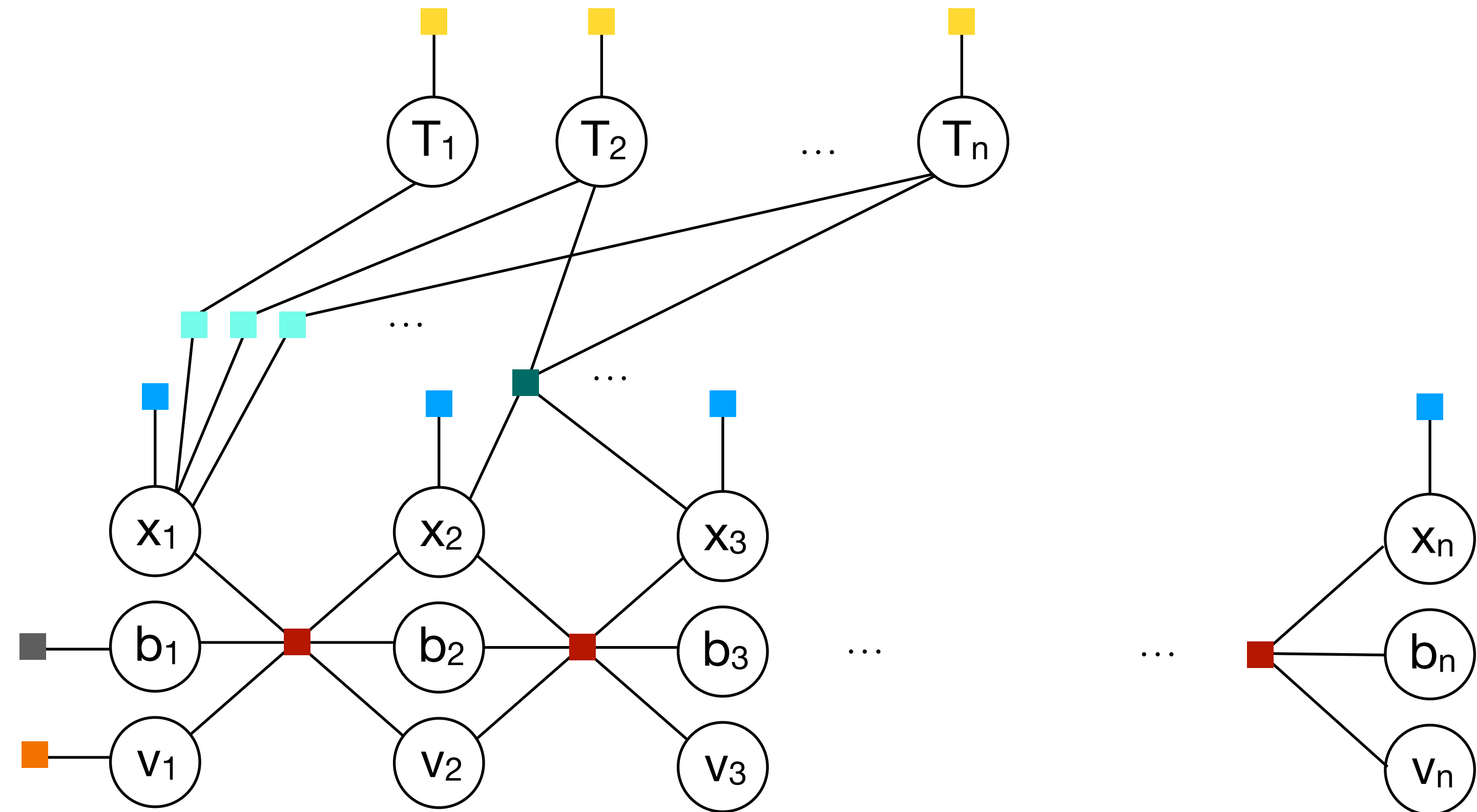
4. Extensions: 3. Sequential Model

- Essential matrix constraint between front and rear facing cameras.
- Capture more data from different viewpoints.
- Add vehicle state variables for robustness to GPS noise and bias.



4. Extensions: 4. IMU Preintegration

- “Preintegration” avoids recomputing the update for each linearization point
- The IMU bias and the vehicle velocity are added to the model.



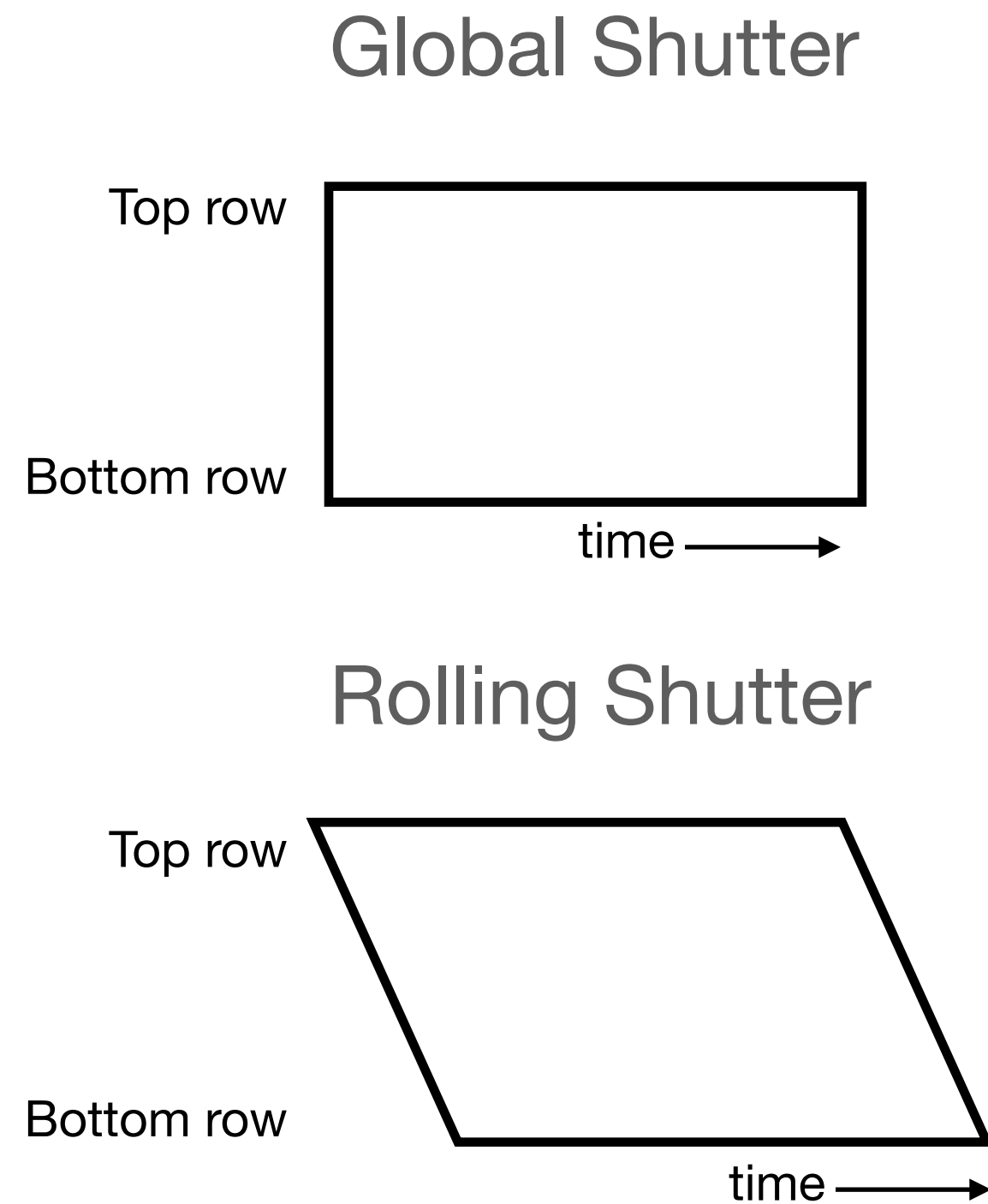
Variables

$T_c \in SE(3)$ camera extrinsic
 $x_t \in SE(3)$ vehicle state
 $b_t \in \mathbb{R}^6$ IMU bias
 $v_t \in \mathbb{R}^3$ velocity

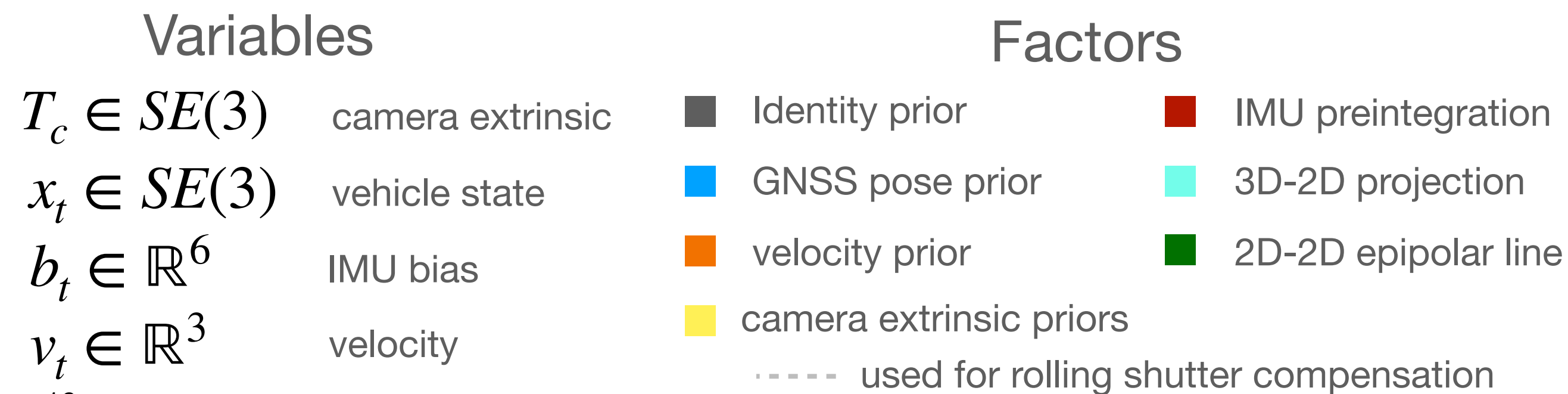
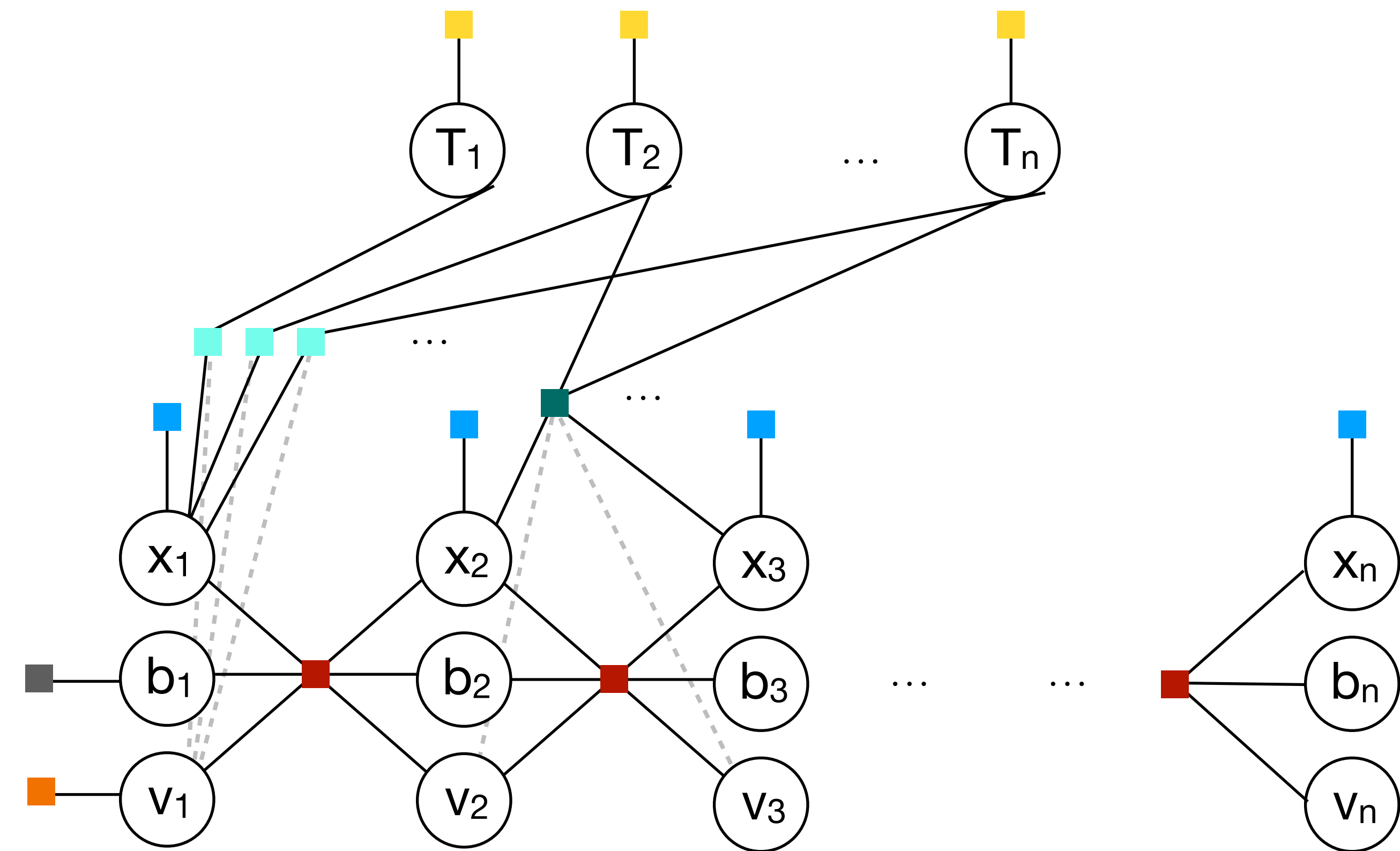
Factors

Identity prior
 GNSS pose prior
 velocity prior
 camera extrinsic priors
 IMU preintegration
 3D-2D projection
 2D-2D epipolar line

4. Extensions: 5. Rolling Shutter Compensation



- Calculate the scan line time using the readout offset and the exposure.
- Interpolate the camera pose for the scan line time for each constraint



5. Evaluation: 1. Metrics

- Residuals. Low in terms of the number of residuals.
- Visual inspection. Accurate alignment quality of multiple cameras.
- Runtime. Two orders of magnitude faster than the previous approach due to the use of an optimization library that exploits sparsity.
- Amount of data. Use the subset of data required for the extrinsic calibration to stabilize.
- Extensible software design. The same implementation was seamlessly applied to different trucks with different camera configurations.

5. Evaluation: 2. Limitations

- Different accuracy in roll, pitch, and yaw
- Data association can be difficult in the long-range camera.
- Multiple sources of error
 - Detection accuracy
 - GPS accuracy
 - Fidelity in map points
 - Perceptual aliasing in data association
 - Extrinsic jitter due to vehicle motion

Questions?